

# Towards $B_s$ Mixing With CDFII

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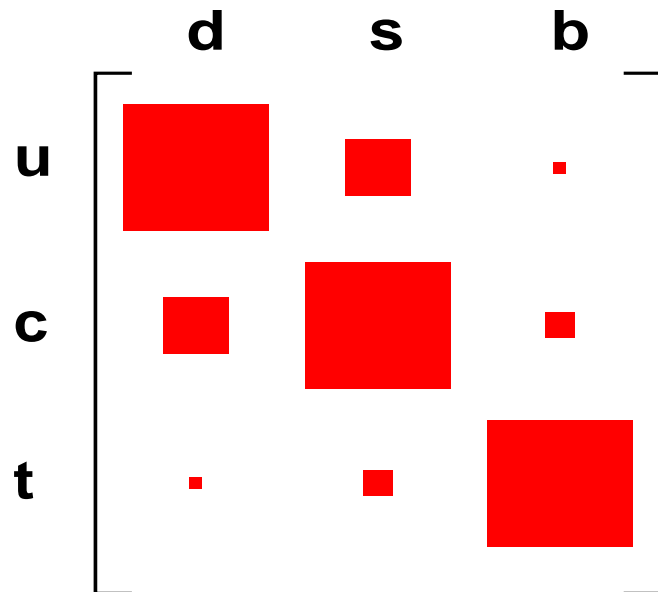
- Tevatron & CDFII
- B mixing measurement setup
- $\text{Br}(B_s^0 \rightarrow D_s^- \pi^+)$
- Prospects

University of Pennsylvania HEP Seminar, Nov 11, 2003

# Introduction/Roadmap

- measurements of  $B^0$  and  $B_s$  mixing contribute to our understanding of weak interactions
  - combined with measurements from B factories, they test the SM
- 
- flagship measurement for CDF II B program
  - overview measurement technique and issues
  - focus on the measurement of  $Br(B_s \rightarrow D_s^- \pi^+)$
  - determines size and properties of our main sample
  - use results of this analysis to project  $B_s$  mixing reach

# Weak Interactions in the SM

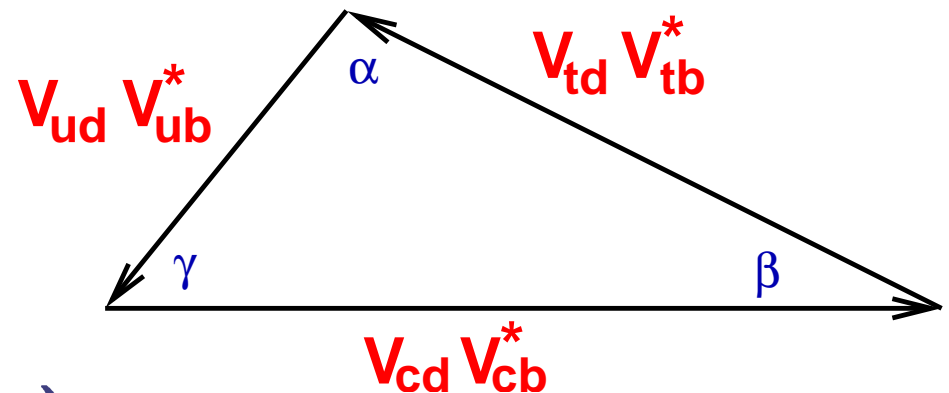


- CKM matrix:  $W^\pm$  boson couplings to quarks
- area  $\sim |V_{ij}|$
- interaction strength  $\sim |V_{ij}|^2$
- unitary matrix:  $VV^\dagger = 1$

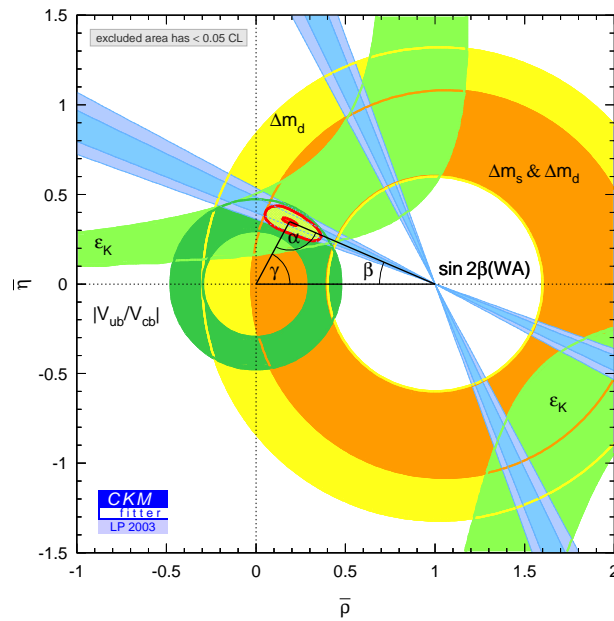
- unitary triangle

- 1 observable phase  
( $\sim$  area,  $\sim$  CP violation)

.. how does  $B_s$  mixing fit into this?



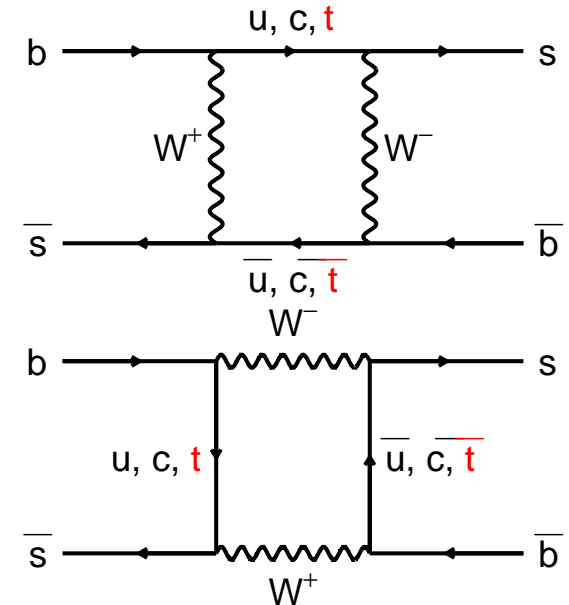
# B Mixing and the Unitarity Triangle



Input for unitarity triangle fits:

- $CP$  violation in kaon system
- $B \rightarrow \pi l \nu X$  vs  $B \rightarrow D l \nu X$
- $B_d, B_s$  meson mixing
- direct measurements of  $\alpha, \gamma$

- both  $B_d$  and  $B_s$  mesons mix
- ratio of mixing frequencies:  
measures one side of the  
unitarity triangle ( $|V_{td}/V_{ts}|$ )
- indir. meas:  $\Delta m_s \leq 24 \text{ ps}^{-1}$
- overconstrain  $\rightarrow$  test SM



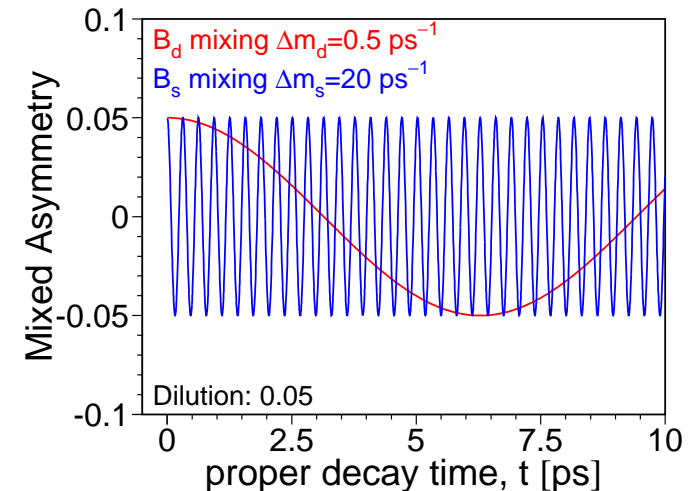
# $B_{(s)}$ Mixing Measurement Ingredients

Per B meson decay,

- determine decay flavor [use **flavor specific states**]
- identify B meson production flavor [**flavor tagging**]
- measure B proper decay time [ **$ct$  resolution**]

Time-dependant asymmetry:

$$\begin{aligned} A_{mix}(t) &= \frac{N_{unmix}^{obs}(t) - N_{mix}^{obs}(t)}{N_{unmix}^{obs}(t) + N_{mix}^{obs}(t)} \\ &= (2p - 1) \cdot \cos(\Delta m \cdot t) \end{aligned}$$



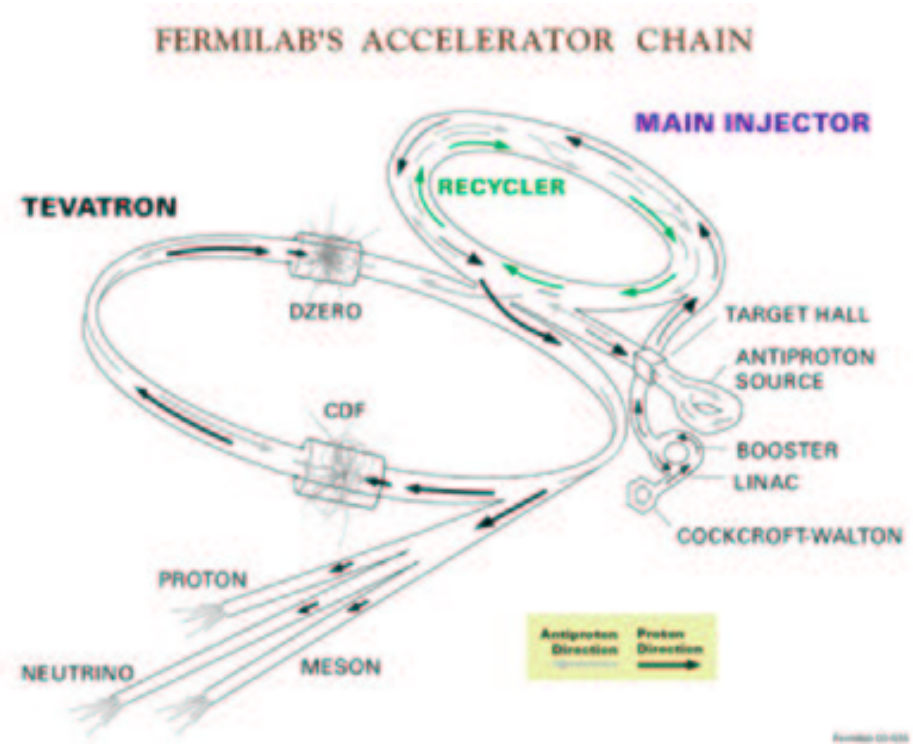
Oscillation amplitude:  $2p - 1 = D$  [**dilution**]

$$\text{Significance} = \sqrt{\frac{\epsilon D^2}{2}} e^{\frac{-(\Delta m)\sigma(c\tau)}{2}} \frac{S}{\sqrt{S+B}}$$

# Apparatus: Tevatron

## Main Injector

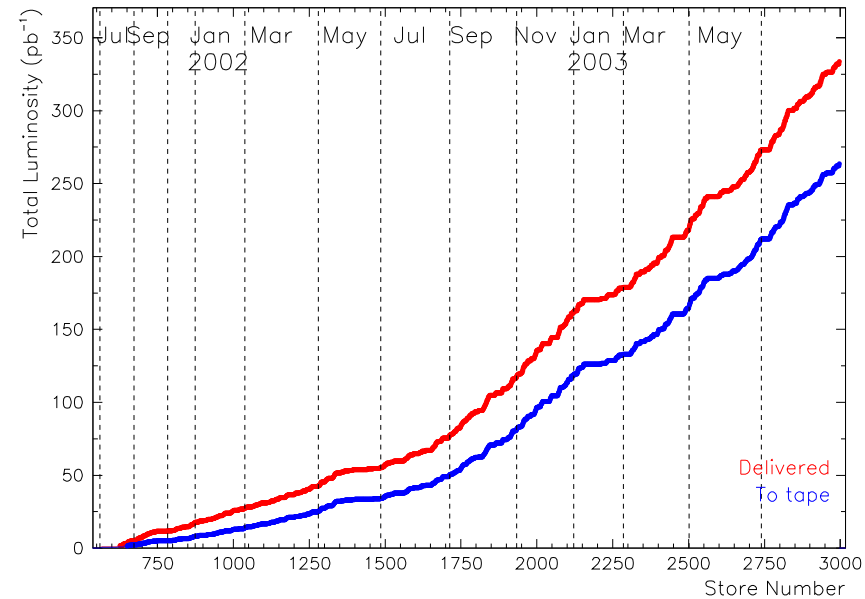
- New injection stage for Tevatron
- Ability to accelerate and deliver higher intensity of protons
- More efficient  $\bar{p}$  transfer
- $\bar{p}$  recycler (in progress)
- Higher Collision rate: 396ns (36x36 bunches)  
⇒ 5-10 Higher Luminosity than Run I
- Higher C.M. Energy:  
Run I: 1.8 TeV → Run II 1.96 TeV



# Tevatron Luminosity

## Tevatron Performance

- Below expectation but improving
  - Record luminosity:  
 $4.8 \times 10^{31} \text{cm}^{-2} \text{s}^{-1}$
  - Now consistently  
 $4 - 7 \text{ pb}^{-1}$  per week



## At CDF:

- $330 \text{ pb}^{-1}$  delivered,  $260 \text{ pb}^{-1}$  recorded
- $\sim 200 \text{ pb}^{-1}$  all important systems on
- analyses shown use  $12 - 120 \text{ pb}^{-1}$   
(depending on when they were done)

# Apparatus: The CDF II Detector

Inherited from Run I:

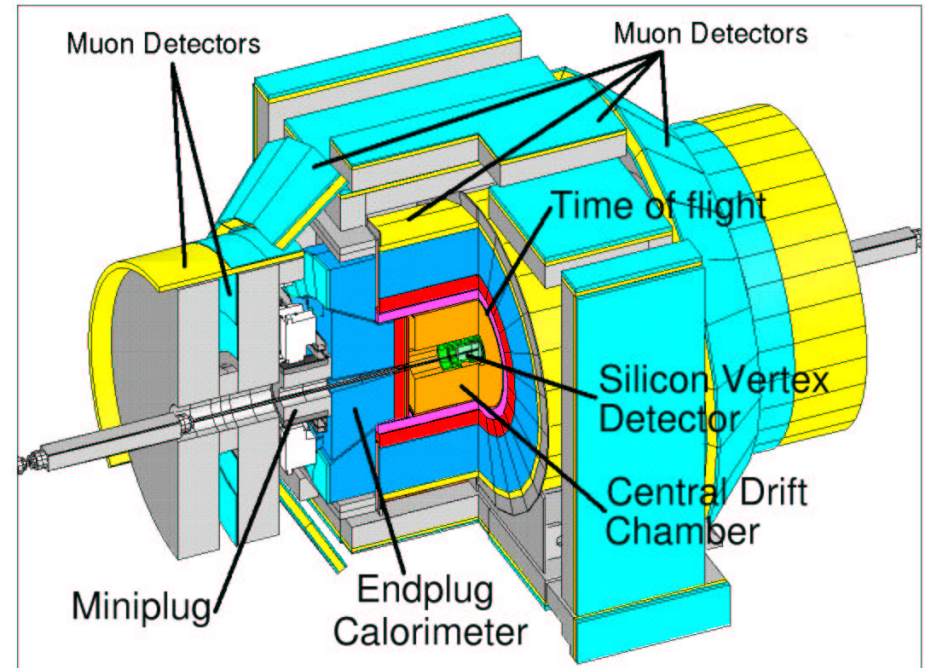
- Central Calor. ( $|\eta| < 1$ )
- Solenoid (1.4 T)

Partially new:

- Muon System  
(extended to  $|\eta| < 2$ )

Completely new:

- 3D Silicon Tracker ( $|\eta| < 2$ )
- Faster Drift Chamber
- Plug and Forward Calorimeters, Time Of Flight
- Trigger System (**trigger on displaced vertices**)





# B Mixing in $p\bar{p}$ collisions

- produce all B species:  $B^0, B^+, B_s, B_c, \Lambda_b$
- huge B production cross section:  $\sim 100 \mu\text{b}$   
(3 – 5  $\mu\text{b}$  “reconstructable”)  
**at  $4 \cdot 10^{31} \text{cm}^{-2} \text{s}^{-1}$ , 150 Hz reconstructable B's**
- large inelastic ( $\sigma \times 1000$ ) background  
 $\Rightarrow$  triggering very important
- B's boosted in the transverse plane (ct measurement)
- less production flavor information than at  $e^+e^-$
- $B^0$  mixing routinely done in Run I

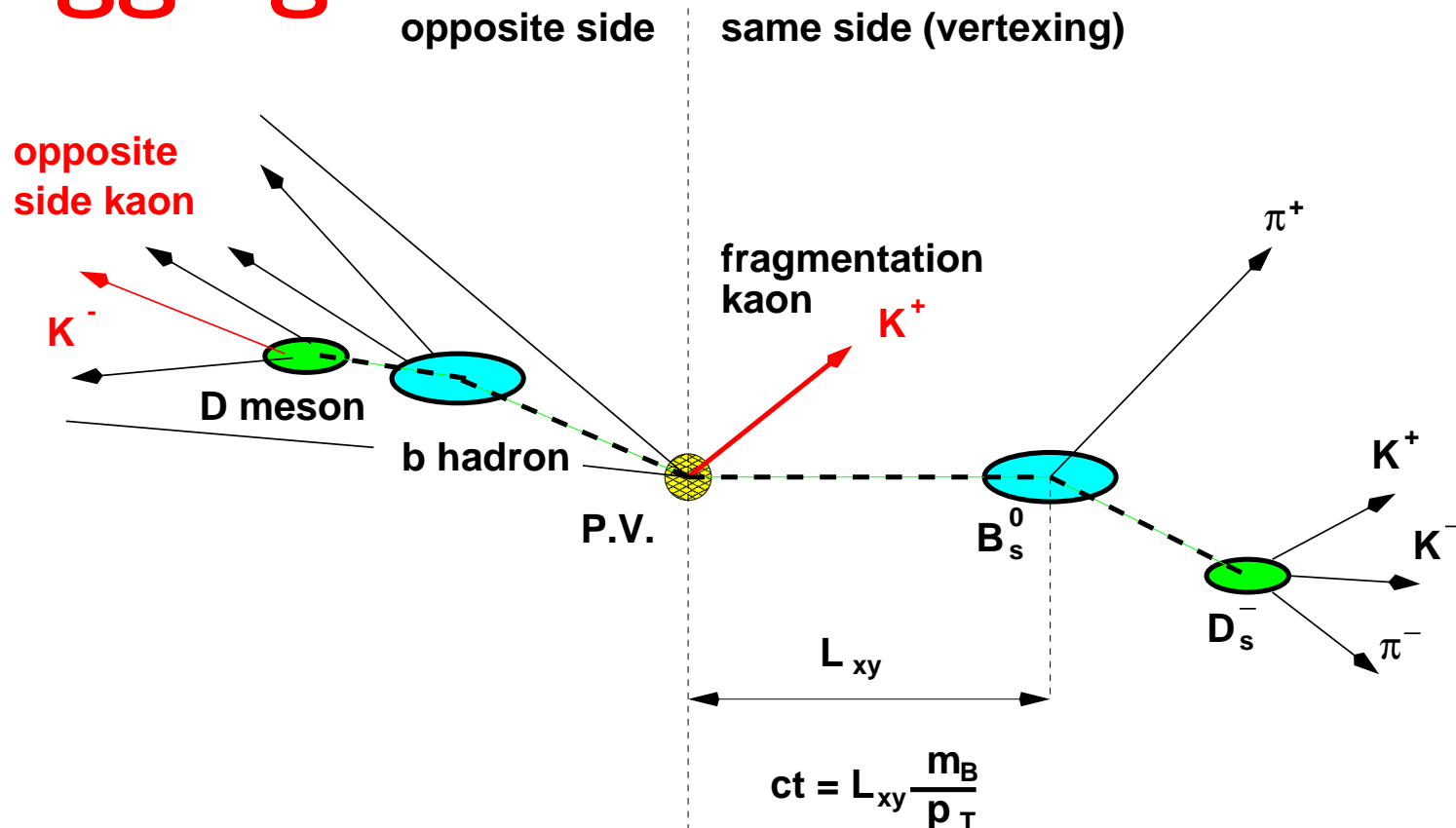
# Reminder: Measurement Ingredients

Per B meson decay,

- determine decay flavor [use **flavor specific** states]
  - identify B meson production flavor [**flavor tagging**]
  - measure B proper decay time [***ct* resolution**]
- 

**Focus: flavor tagging techniques**

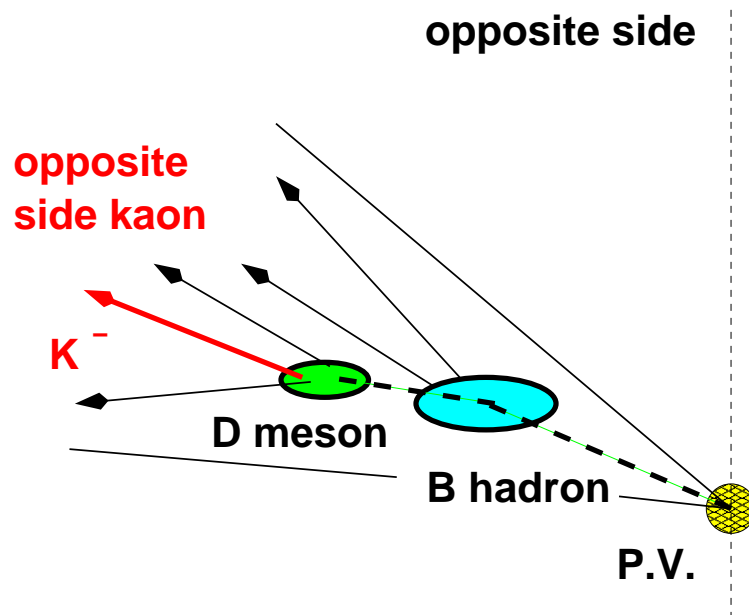
# Tagging The Production Flavor



- **Tagging** algorithms identify B production flavor
- **Opposite Side Tagging:** B's produced in pairs, identify the flavor of the opposite B meson
- **Same Side Tagging:** hadronization  $\pi/K$  charge is correlated to  $B_d/B_s$  production flavor

# Tagging: Opposite Side Tagging

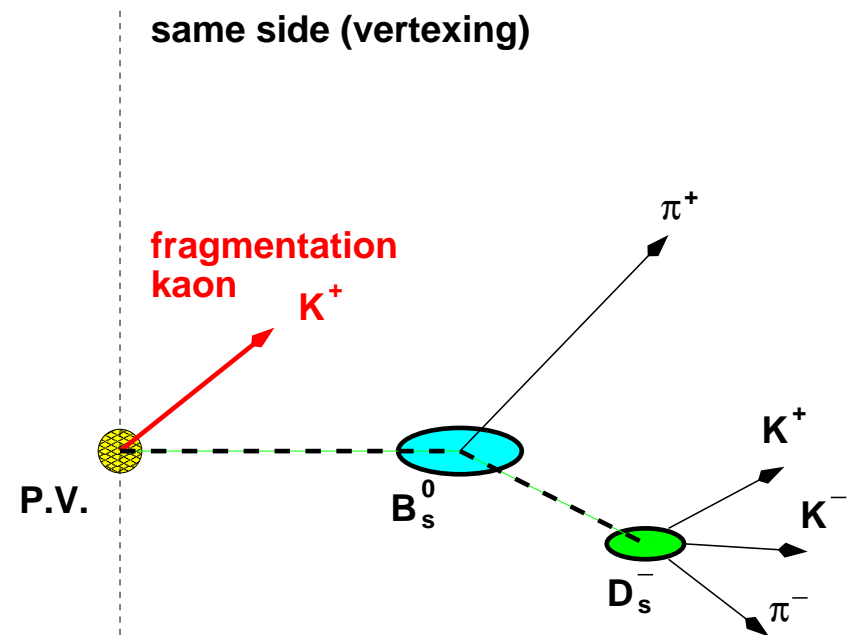
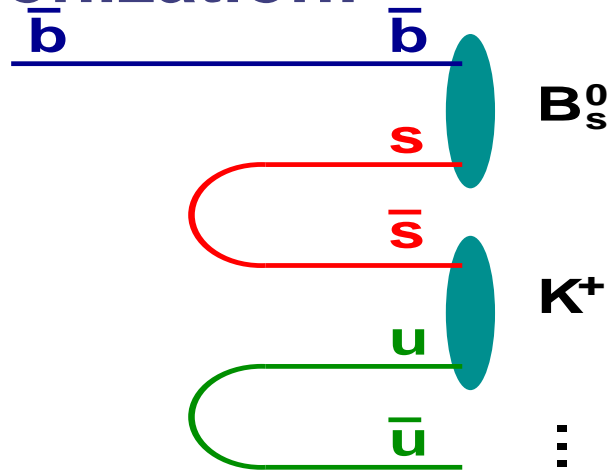
- **Lepton Tagging:** find lepton from  $B \rightarrow Dl\nu X$
- **Jet Charge Tagging:** momentum-weighted sum of track charge in B jet (+ displacement)
- **Kaon Tagging:** assume  $b \rightarrow c \rightarrow s$  decay, find kaon in B jet



- Difficulties with OST:
- 20-40% opposite side B's outside detector acceptance
- $B^0, B_s^0$  mix  $\rightarrow$  production flavor information lost

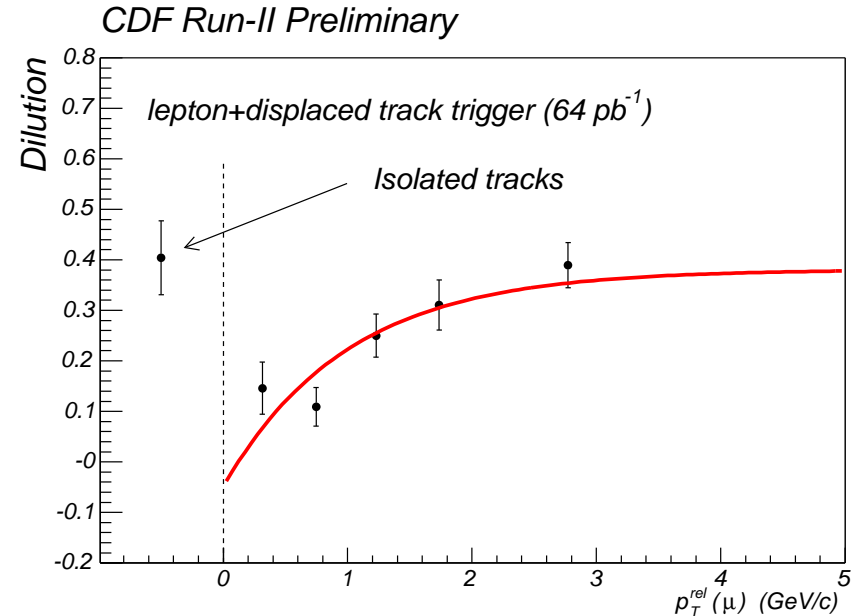
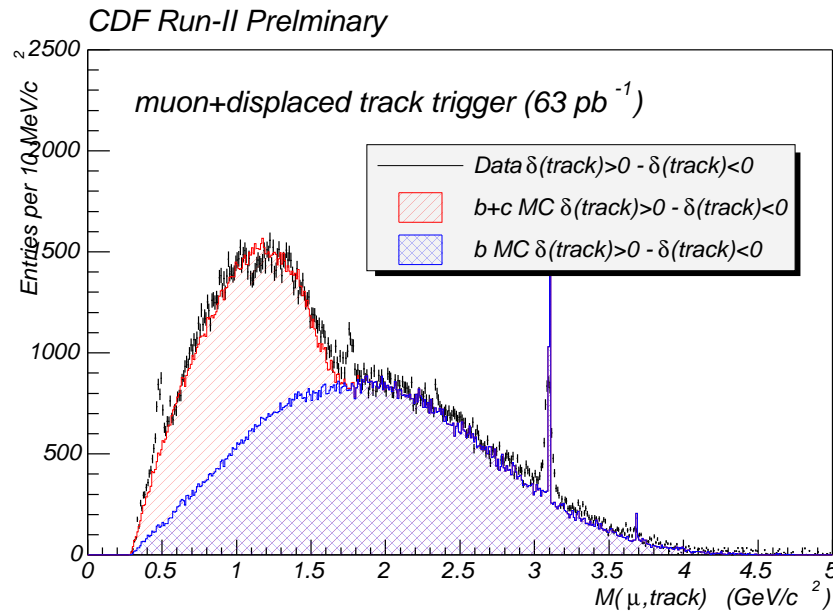
# Tagging: Same Side Tagging

Exploit signature of  $B_s$  hadronization:



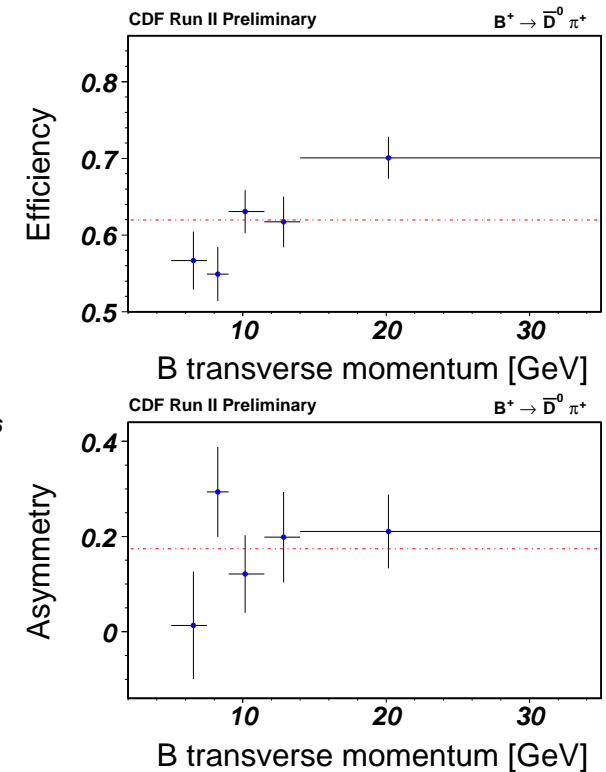
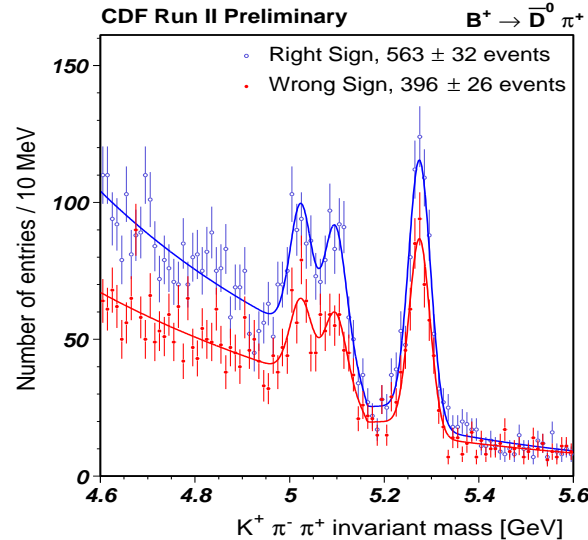
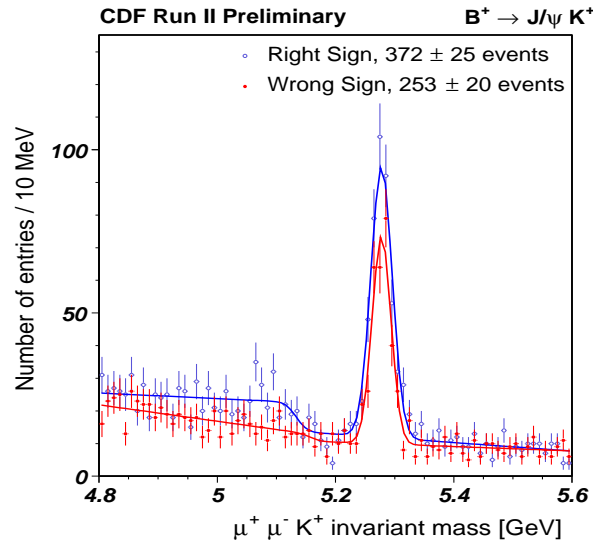
- 80% of tracks in event are pions [kaons  $\sim 10\%$ ]
- fragmentation tracks are soft  $\rightarrow$  TOF particle ID
- Run I  $B^0$  mixing using pion SST
- expect improvement using TOF particle ID
- combined (OST + SST) tagging power:  $\epsilon D^2 \sim 5\%$

# Tagging Efforts in Run II



- trigger on lepton + displaced track (SVT)
- signal:  $l$ -track intersection  $ct > 0$
- background:  $l$ -track intersection  $ct < 0$
- require  $2 \text{ GeV}/c < m(l, \text{track}) < 4 \text{ GeV}/c$
- $\sim 500\text{k}$  inclusive B decays  $\rightarrow$  test taggers
- example: measure dilution of soft muon tag

# Tagging Efforts in Run II (cont)



- fully reconstructed  $B^+$  decays
- measure efficiency and dilution
- example: same side pion tag
- $B^+ \rightarrow J/\psi K^+$ :  $\epsilon D^2 = 2.4 \pm 1.2(stat)\%$
- $B^+ \rightarrow \bar{D}^0 \pi$ :  $\epsilon D^2 = 1.9 \pm 0.9(stat)\%$
- Run I  $J/\psi K^*$ :  $\epsilon D^2 = 1.8 \pm 0.4(stat)\%$

# Reminder: Measurement Ingredients

Per B meson decay,

- determine decay flavor [use **flavor specific** states]
  - identify B meson production flavor [**flavor tagging**]
  - measure B proper decay time [ **$ct$  resolution**]
- 

## Focus: $ct$ Resolution

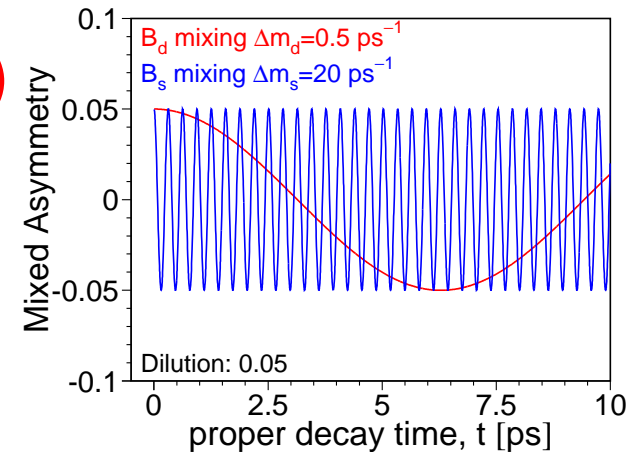
- importance of  $ct$  resolution
- triggering on fully hadronic B (and charm) decays
- digression:  $D$  meson mass difference measurement
- rate of fully hadronic  $B_s$  decays
- $\Rightarrow$  mixing reach projection



# Precise $ct$ Measurements

- rapid oscillations:  
 $\Delta m_s \geq 13.1 \text{ ps}^{-1}$  (90%CL, PDG)  
(indir. meas:  $\leq 24 \text{ ps}^{-1}$ )
- very good  $ct$  resolution needed:

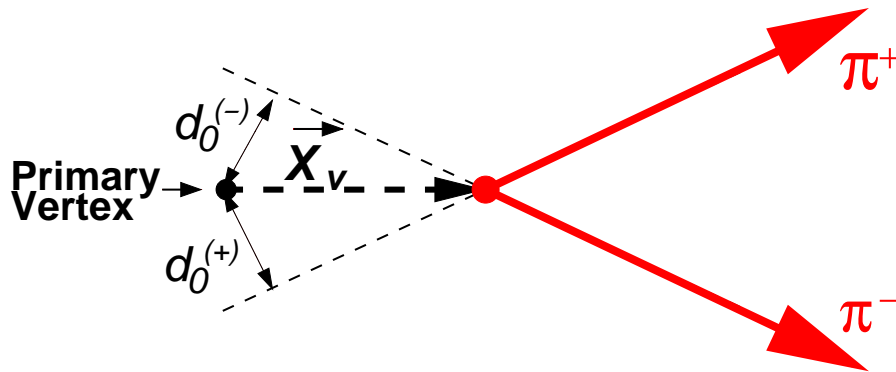
$$\sigma_{ct} = \left( \frac{\sigma_L}{\gamma\beta} \right) \oplus \left( \frac{\sigma_{\gamma\beta}}{\gamma\beta} \right) \cdot ct$$



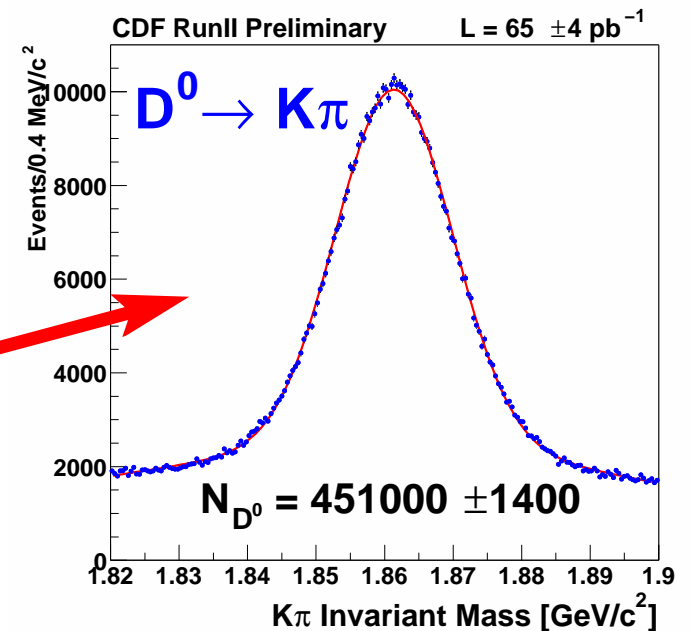
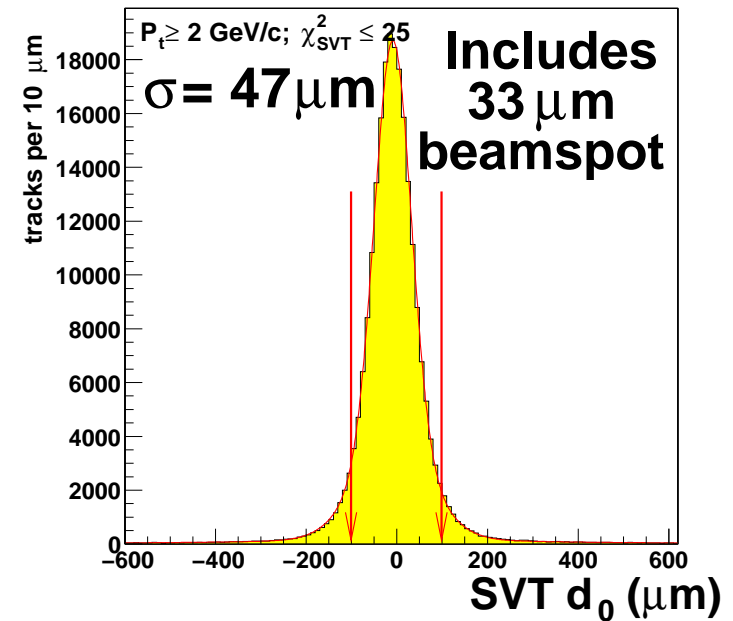
- semileptonic decays: B momentum error  $\sim 15\%$
- hadronic decay ( $B_s \rightarrow D_s \pi$ ) negligible ( $\sim 0.5\%$ )
- using base RunII silicon : 60 fs  $\Delta m_s \sim 17 \text{ ps}^{-1}$
- layer of Si on beampipe: 45 fs  $\Delta m_s \sim 22 \text{ ps}^{-1}$
- **Problem: how do we trigger on these decays?**

# Triggering on displaced tracks

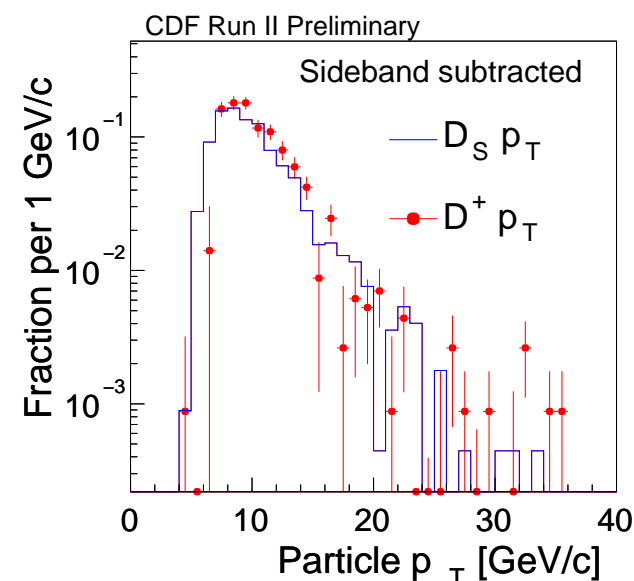
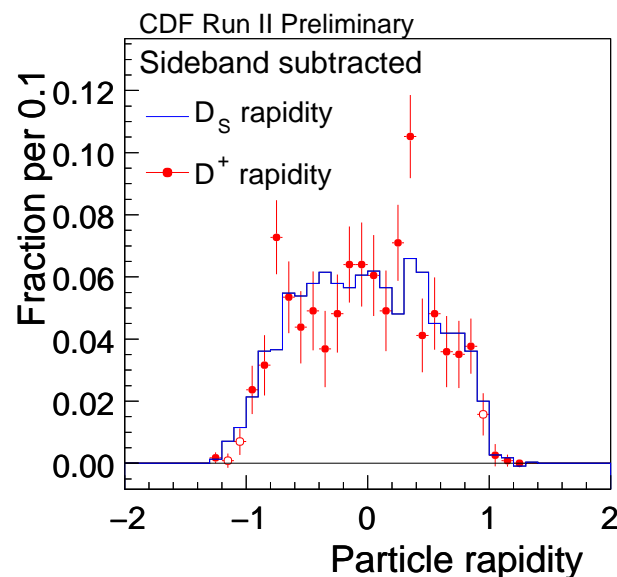
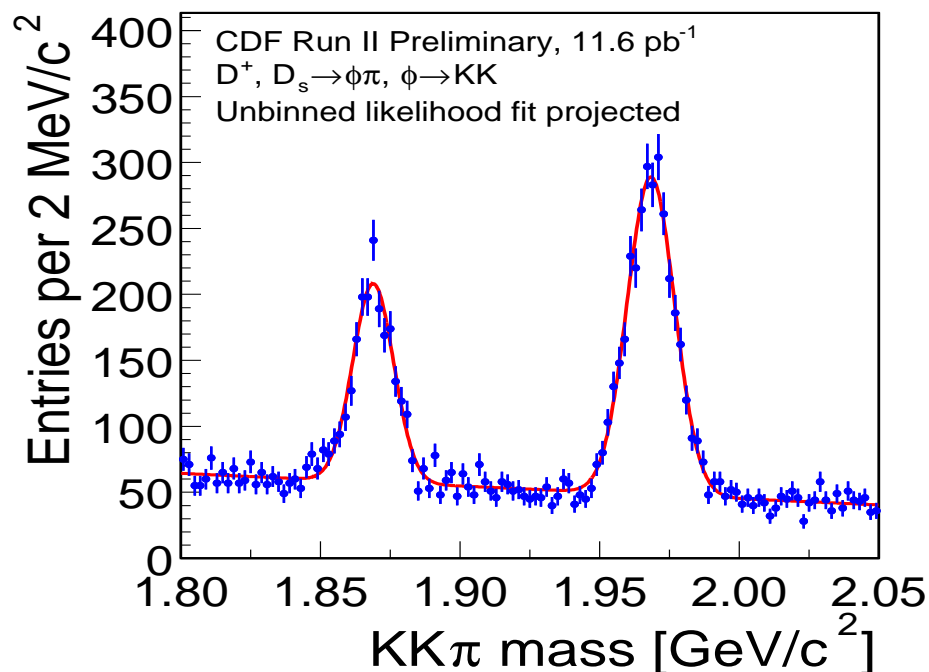
- trigger  $B \rightarrow \pi\pi, B_s \rightarrow D_s\pi$
- challenge: read out SVX and track at 10's of kHz  $\rightarrow$  SVT



- trigger on 2 displaced tracks  
( $p_T > 2 \text{ GeV}/c, 120 \mu\text{m} < |d_0| < 1 \text{ mm}$ )
- huge charm samples gathered
- with small int. luminosity, competitive charm analyses



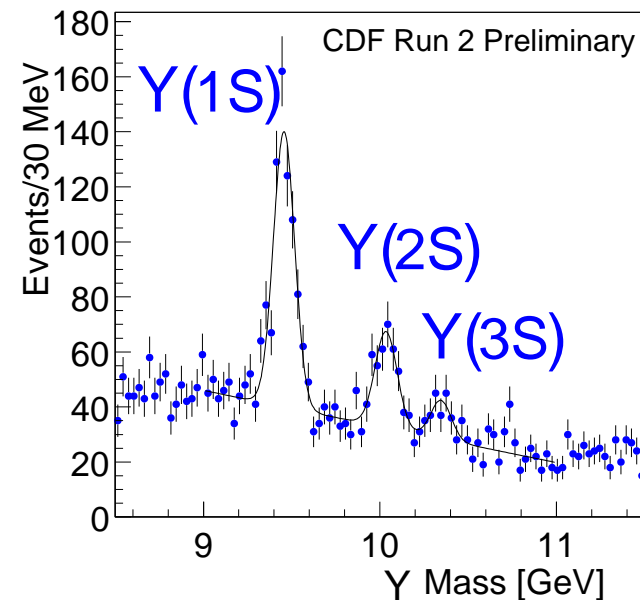
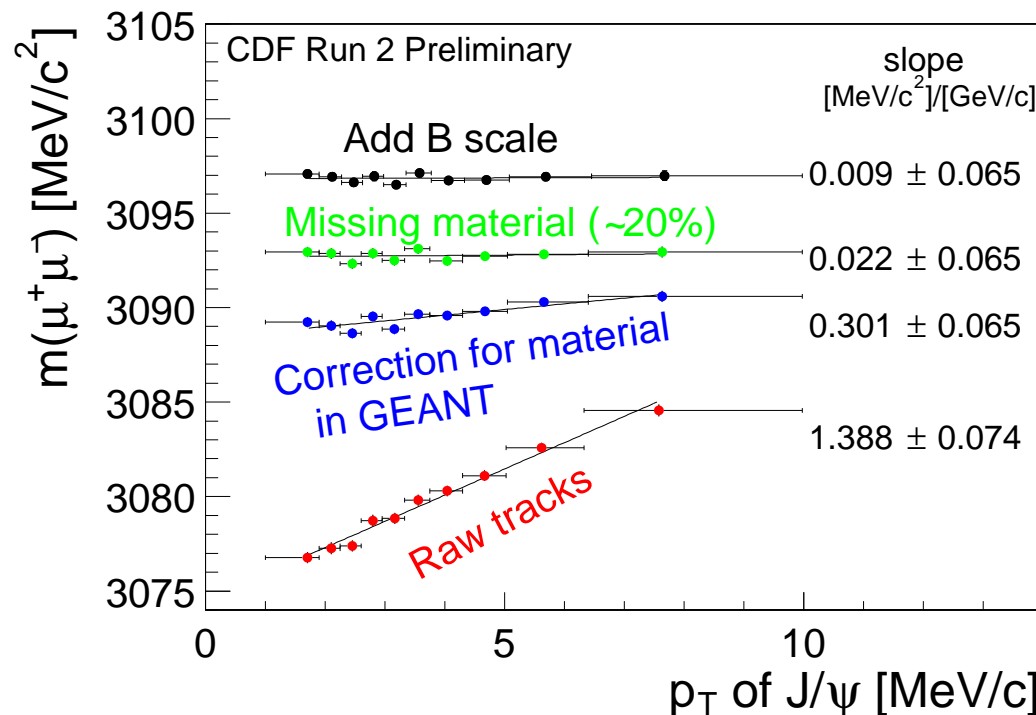
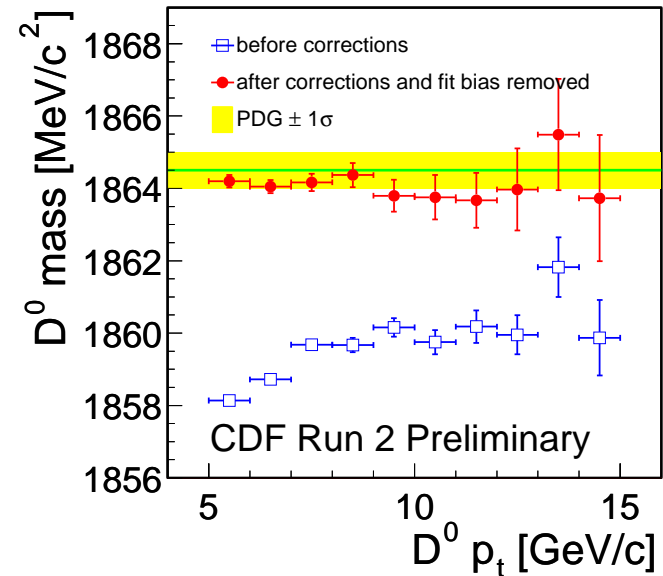
# D Meson Mass Difference



- 1.4k D<sup>+</sup>, 2.4k D<sub>s</sub><sup>+</sup> → φπ<sup>+</sup>
- mass resolution ∼ 8 MeV/c<sup>2</sup>
- similar kinematics
- expect small syst. errors

# Momentum Scale Calibration

- study  $J/\psi$ 's to calibrate:
  - energy loss in detector
  - magnetic field value
- crosscheck with other decays



# Mass Difference Result

$$m(D_s^+) - m(D^+) = 99.41 \pm 0.38(stat) \pm 0.21(syst) \text{ MeV}/c^2$$

PRD 68 (2003) 072004 - First Tevatron Run II publication

systematics small, dominated by bkg model:

Effect	Syst. [MeV/c <sup>2</sup> ]
fitting	0.14
event selection	0.11
momentum scale	0.10
tracker effects	0.06
calibration procedure	0.03
Total	0.21

- PDG '02:  $99.2 \pm 0.5 \text{ MeV}/c^2$
- CLEO2 (1998):  $99.5 \pm 0.6 \pm 0.3 \text{ MeV}/c^2$
- BaBar (2002):  $98.4 \pm 0.1 \pm 0.3 \text{ MeV}/c^2$

# Reminder: Measurement Ingredients

Per B meson decay,

- determine decay flavor [use **flavor specific** states]
  - identify B meson production flavor [**flavor tagging**]
  - measure B proper decay time [***ct* resolution**]
- 

Focus: Rate of fully reconstructed  
hadronic  $B_s$  decays

- use as input for mixing reach projection

# Fully Hadronic $B_s$ decays

- good for  $B_s$  mixing because of good  $ct$  resolution
- $B_s^0 \rightarrow D_s^- \pi^+$  “golden mode”
  - fully hadronic, flavor specific
  - few tracks  $\rightarrow$  “easy” to trigger, reconstruct
  - $D_s^- \rightarrow \phi^0 \pi^-$ ,  $\phi^0 \rightarrow KK$  narrow resonance  
(cut on  $KK$  invariant mass  $\rightarrow$  good  $S/N$ )
- first observed at LEP
- branching fraction? (PDG:  $<13\%$ , 95% CL)  
(determines number of  $B_s$  available for mixing)
- initially assumed  $\sim Br(B^0 \rightarrow D^- \pi^+)$
- background composition?  $S/B$ ?
- **answers: branching fraction measurement**

# Rate of $B_s$ vs $B^0$

- want to understand rate of  $B_s \rightarrow D_s^- \pi^+$
  - compare to similar decay  $B^0 \rightarrow D^- \pi^+$
  - count how many  $B_s$  vs  $B^0$  are reconstructed
  - **what is different?**
- 
- rate of  $B_s$  production different from  $B^0$
  - $f_s/f_d$  probability for  $b$  to hadronize as  $B_s/B^0$
- 
- final state  $D_s \rightarrow \phi \pi$  vs  $D^- \rightarrow K^+ \pi^- \pi^-$
  - account for by using PDG ratio of BR's
- 
- kinematics slightly different  $\rightarrow$  efficiency?
  - $\epsilon = \epsilon(acc) \cdot \epsilon(det) \cdot \epsilon(trig) \cdot \epsilon(rec)$
  - will need to consult Monte Carlo simulation for this



# $Br(B_s^0 \rightarrow D_s^- \pi^+)$ Measurement:

We measure the ratio of branching fractions:

$$\frac{f_s}{f_d} \cdot \frac{Br(B_s^0 \rightarrow D_s \pi)}{Br(B^0 \rightarrow D^- \pi)} = \frac{N(B_s^0)}{N(B^0)} \cdot \frac{\epsilon(B^0)}{\epsilon(B_s^0)} \cdot \frac{Br(D^+ \rightarrow K \pi \pi)}{Br(D_s \rightarrow \phi \pi, ..)}$$

- control sample:  $B^+ \rightarrow \overline{D}^0 \pi^+$  and corresponding BR relative to  $B^0 \rightarrow D^- \pi^+$
- $N(B_s^0)$ ,  $N(B^+)$ ,  $N(B^0)$  obtained from fits to data
- $\epsilon(B^0) / \epsilon(B_s^0)$ ,  $\epsilon(B^0) / \epsilon(B^+)$  from realistic MC
- $BR(D^- / D_s^- / D^0)$  are taken from PDG

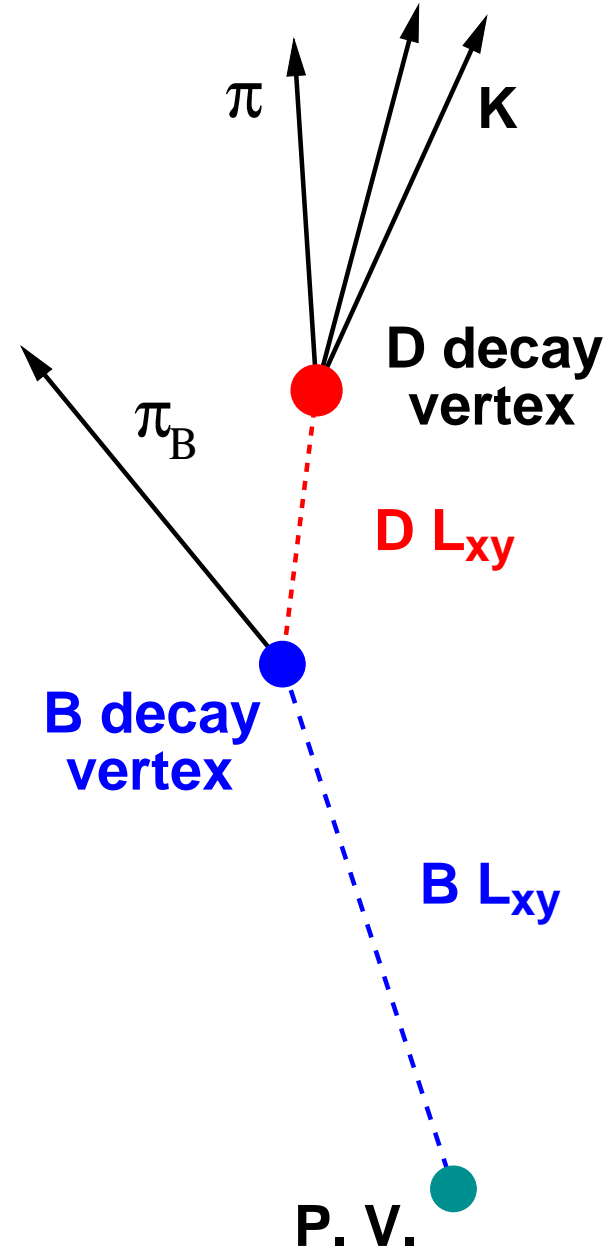
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## Key issues:

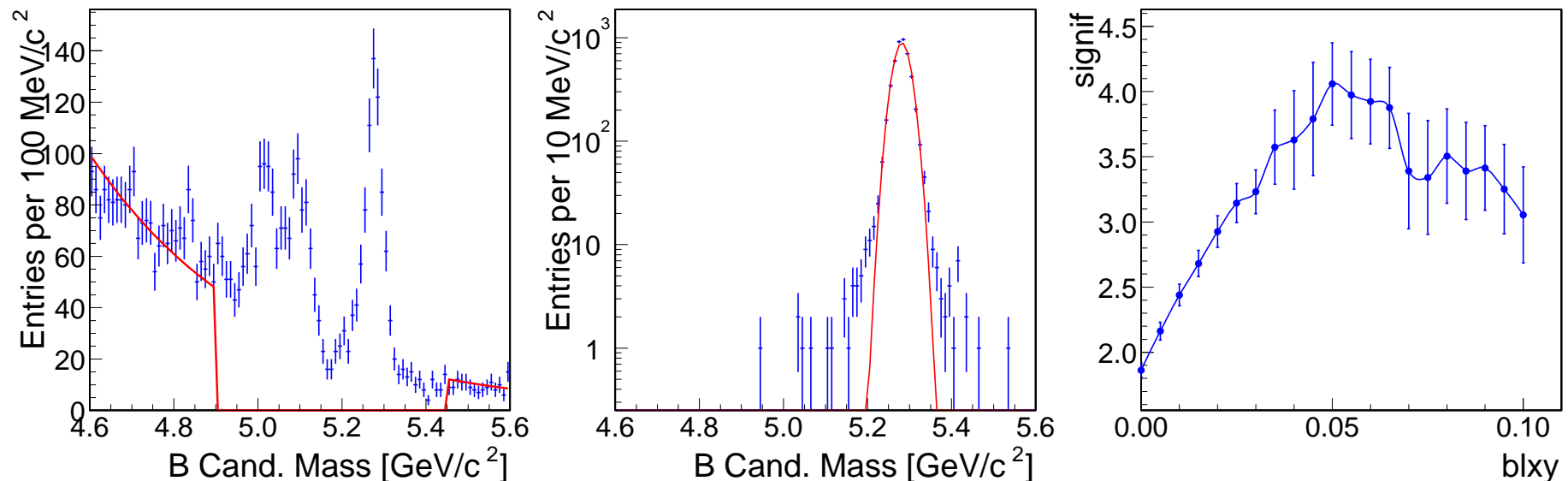
- reconstruction of  $B$  mesons with good  $S/B$
- robust and correct extraction of  $N(B)$
- realistic trigger and analysis simulation

# Typical $B$ meson selection cuts:

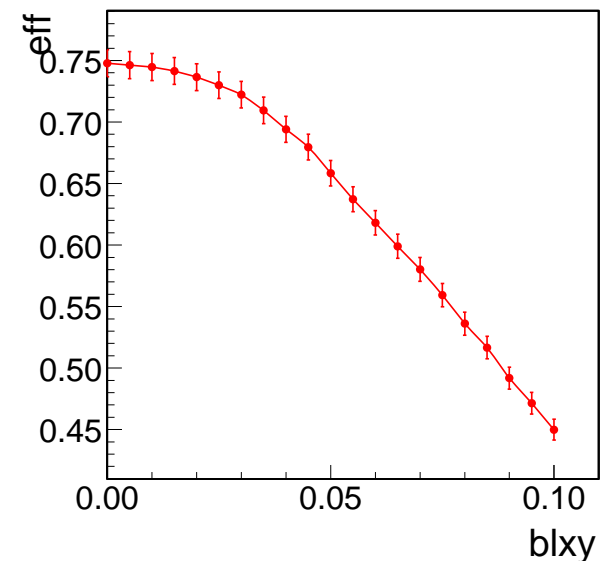
- $\chi^2_{r,\varphi}(D) < 14$
- $\chi^2_{r,\varphi}(B) < 15$
- $p_T(D) > 3.5 \text{ GeV}/c$
- $p_T(B) > 5.5 \text{ GeV}/c$
- $L_{xy}(B) > 400 \mu\text{m}$
- $L_{xy}(B \rightarrow D) > -150 \mu\text{m}$
- $\Delta R(D, \pi_B) < 1.5$
- $p_T(\pi_B) > 1.6 \text{ GeV}/c$
- $|d_0(B)| < 80 \mu\text{m}$
- $\phi^0$  mass cut for  $B_s^0$   
(  $1010 \text{ MeV}/c^2 < m(\phi^0) < 1028 \text{ MeV}/c^2$  )



# B Meson Selection Optimization:

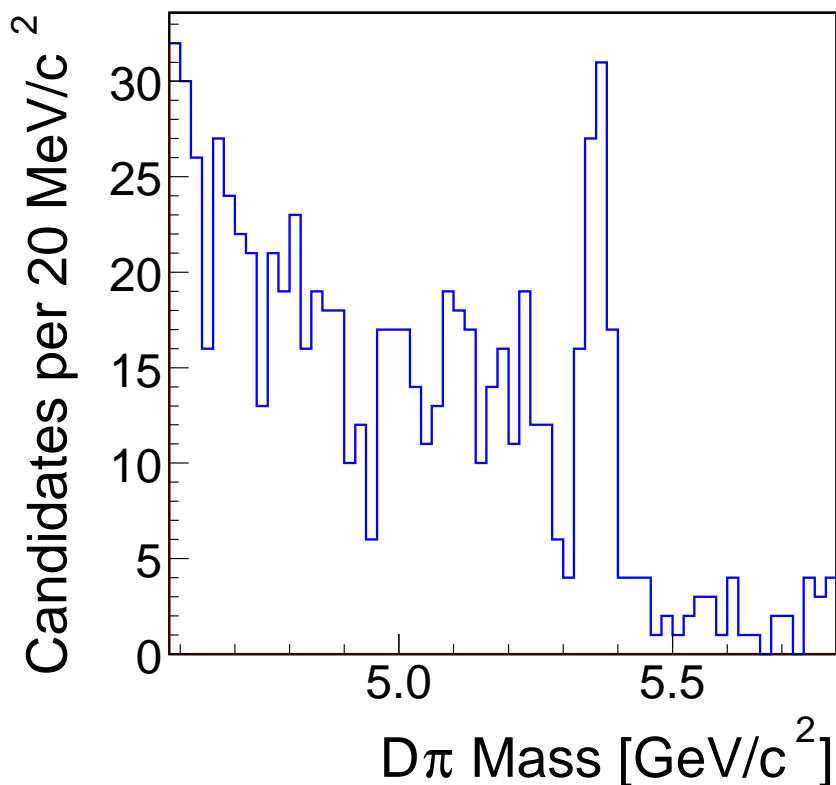


- optimize  $S/\sqrt{S+B}$
- keep efficiency high
- background estimate from data
- signal estimate from scaled MC
- similar cuts from both studies

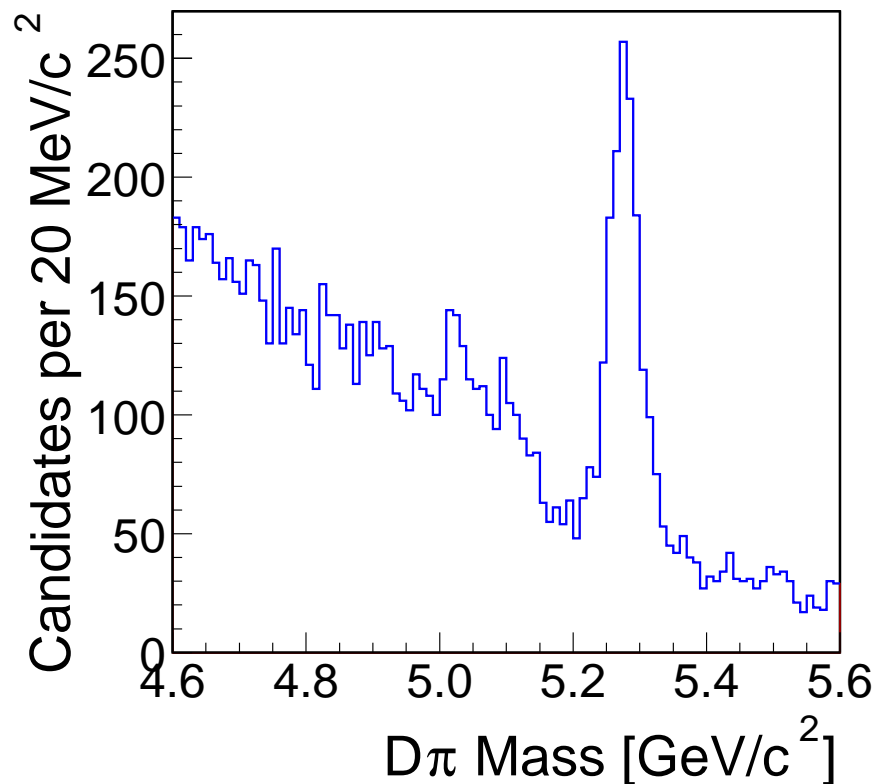


# B Meson Mass Spectra:

$$B_s^0 \rightarrow D_s^- \pi^+$$

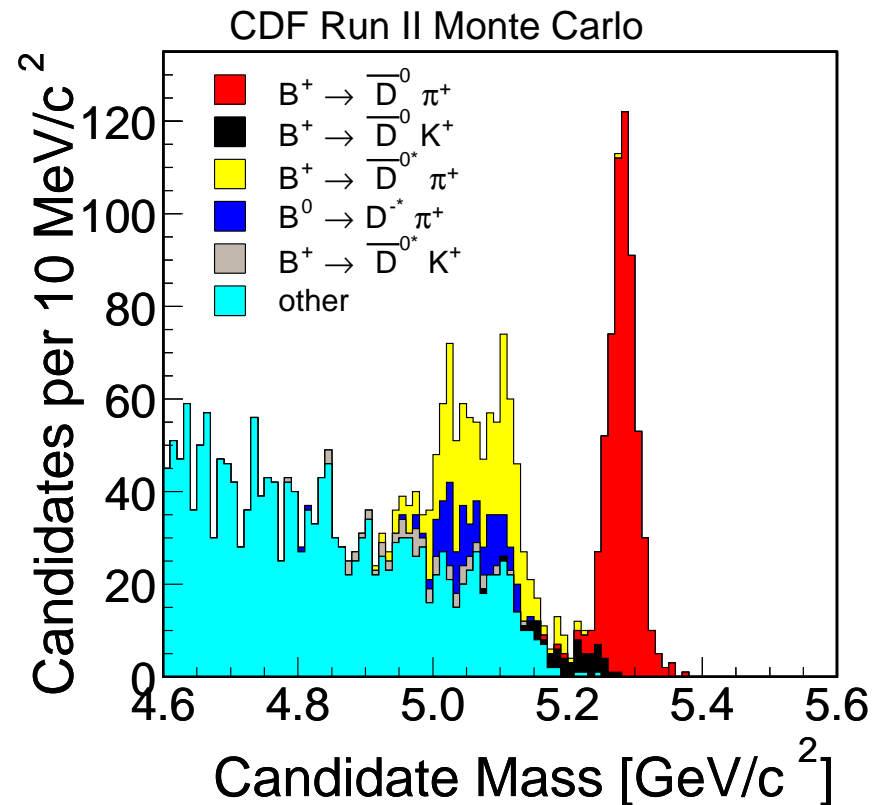
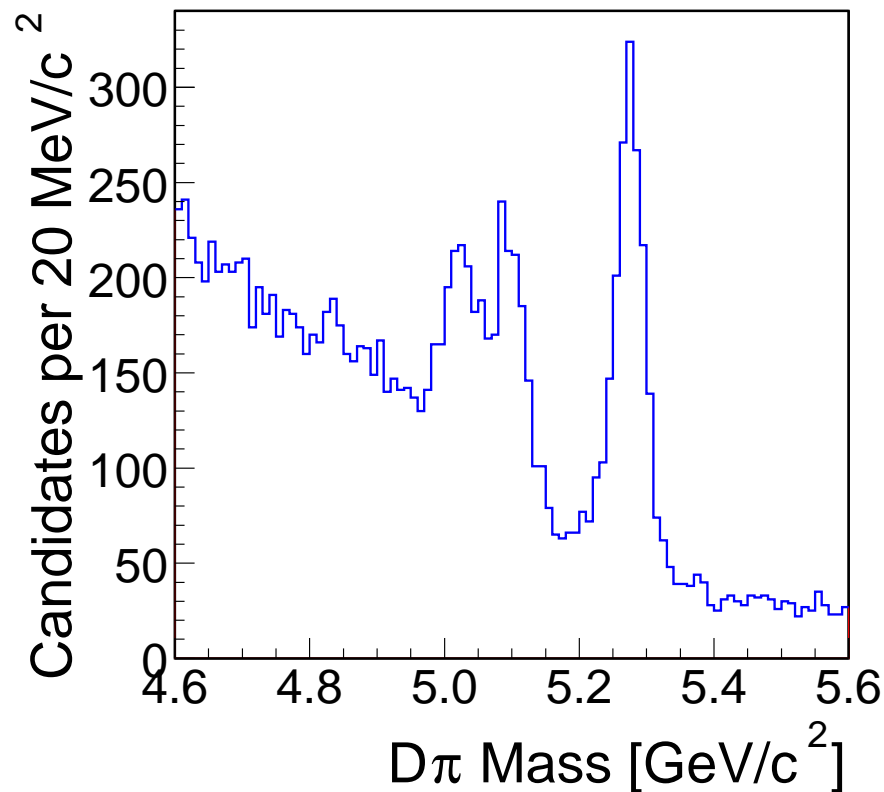


$$B^0 \rightarrow D^- \pi^+$$



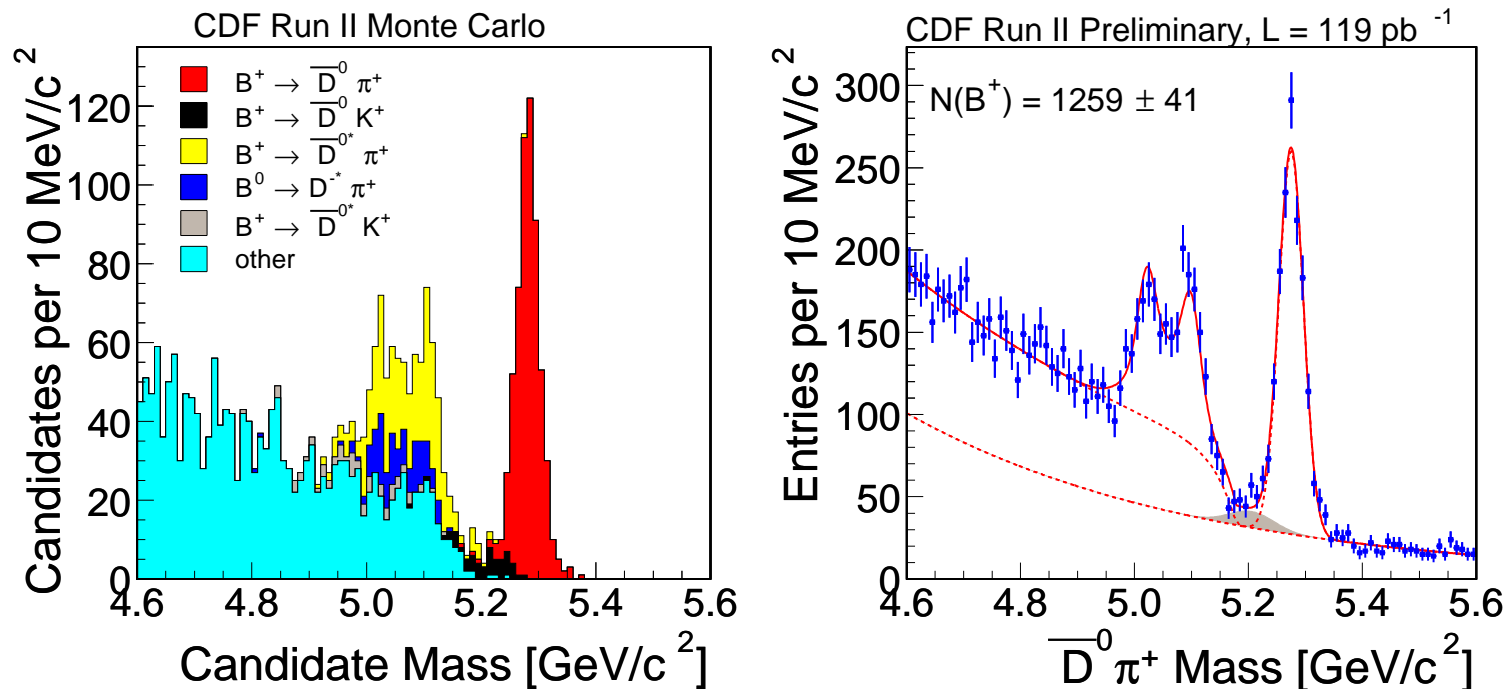
- $B$  mass peaks are quite clean ( $S/N > 2 : 1$ )
- spectra have interesting structures
- use Monte Carlo to study background shapes

# Background Shapes ( $B^+ \rightarrow \overline{D}^0 \pi^+$ )



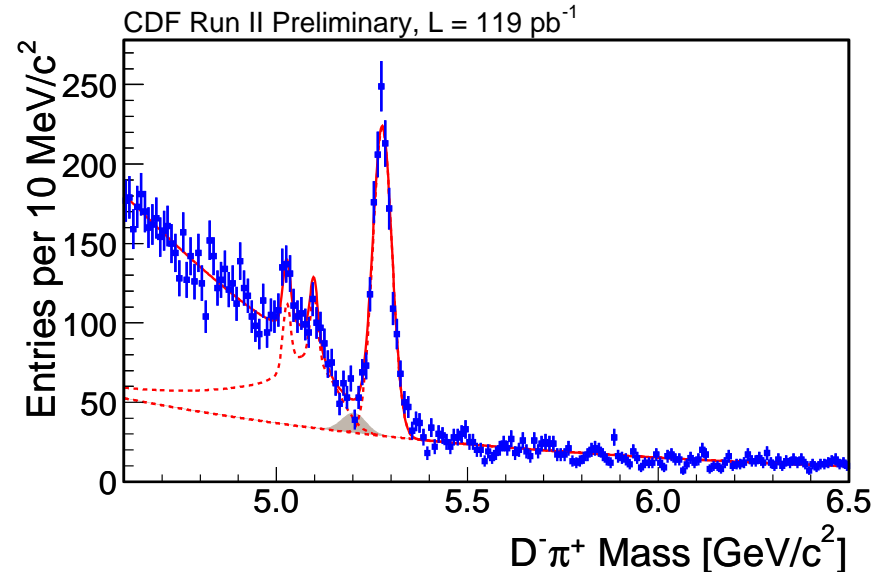
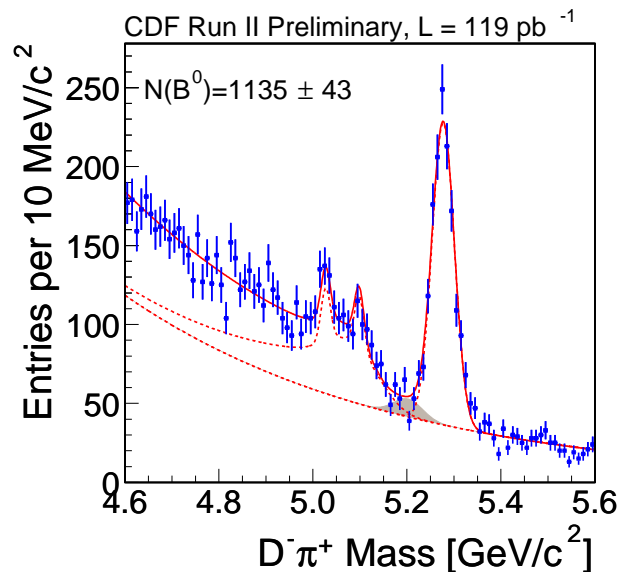
- Monte Carlo:  $B \rightarrow \overline{D}^0 X, \overline{D}^0 \rightarrow K^+ \pi^-$
- GEANT simulation of detector response
- realistic trigger simulation
- spiky structures are signatures of  $D^*$  polarization

# Fitting With Templates:



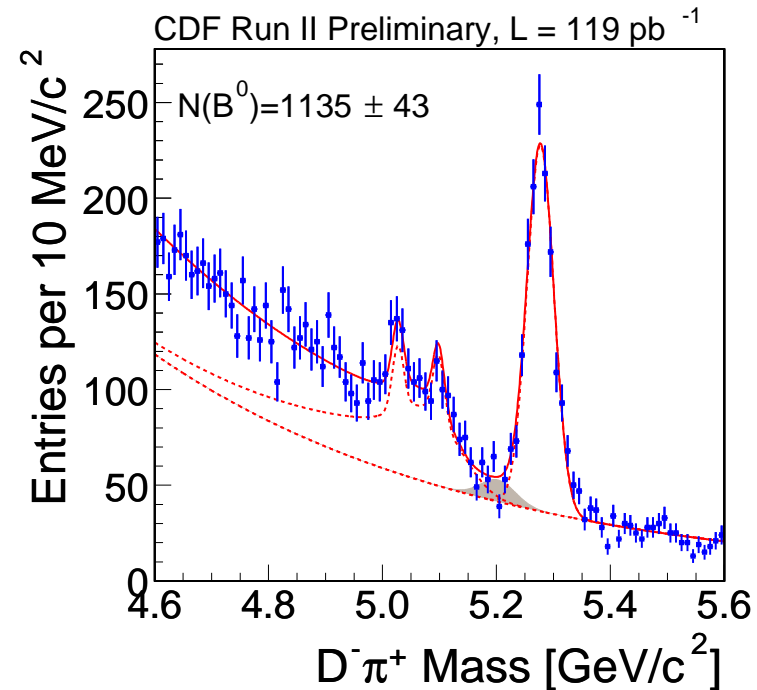
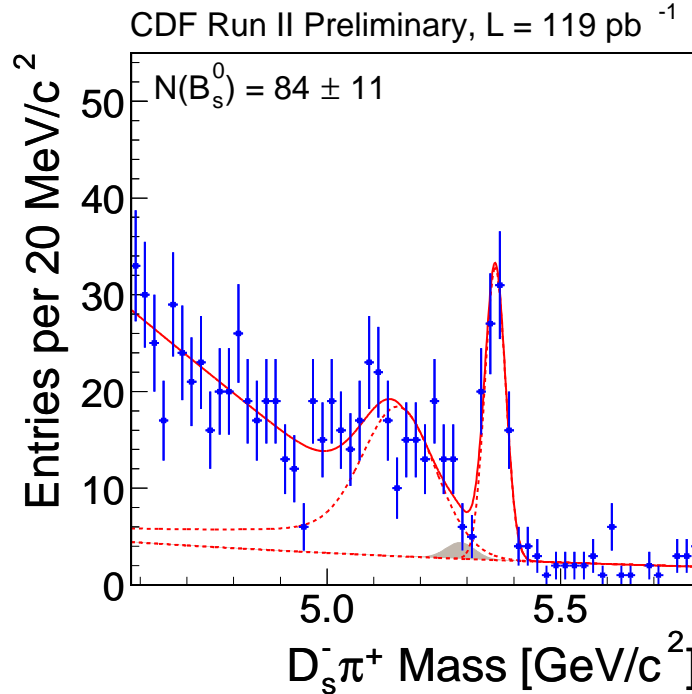
- decompose background into groups with similar features (spiky, Cabbibo suppressed, ..)
- based on Monte Carlo, create analytical templates
- extract shape parameters from MC
- keep shape parameters fixed in fit to data
- combinatorial background  $\rightarrow$  single exponential

# Fit Result N(B) Stability



- how reliable is our counting method?  
(assign counting systematic error)
- vary shape parameters for templated background
- extend fit range, fix continuum parametrization
- fits result change up to  $\sim 7\%$
- can improve background parametrization

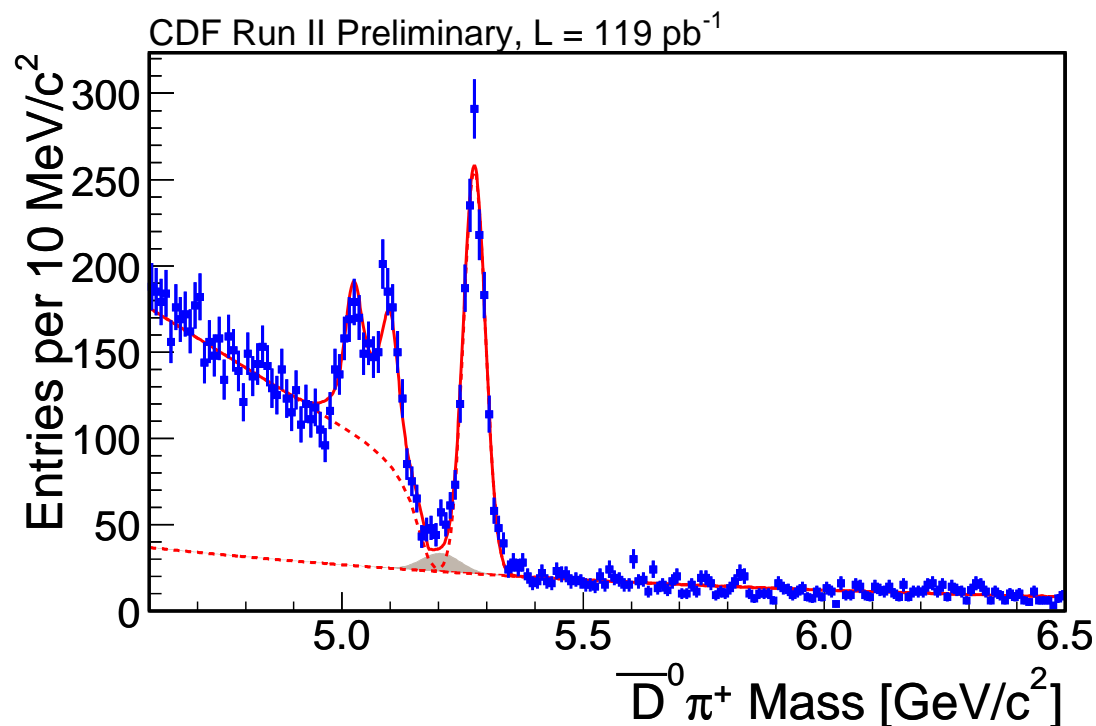
# Fit Results for $B_s^0$ and $B^0$



- counting systematic error  $\sim 7\%$
- $84 \pm 11(\text{stat}) \pm 4(\text{syst})$   $B_s$  candidates
- $1135 \pm 43(\text{stat}) \pm 80(\text{syst})$   $B^0$  candidates
- this determines the ratio  $N(B_s)/N(B_d)$
- remaining work: correct for detector effects  
(different efficiencies for  $B_s, B^0$ )  $\Rightarrow$  from MC

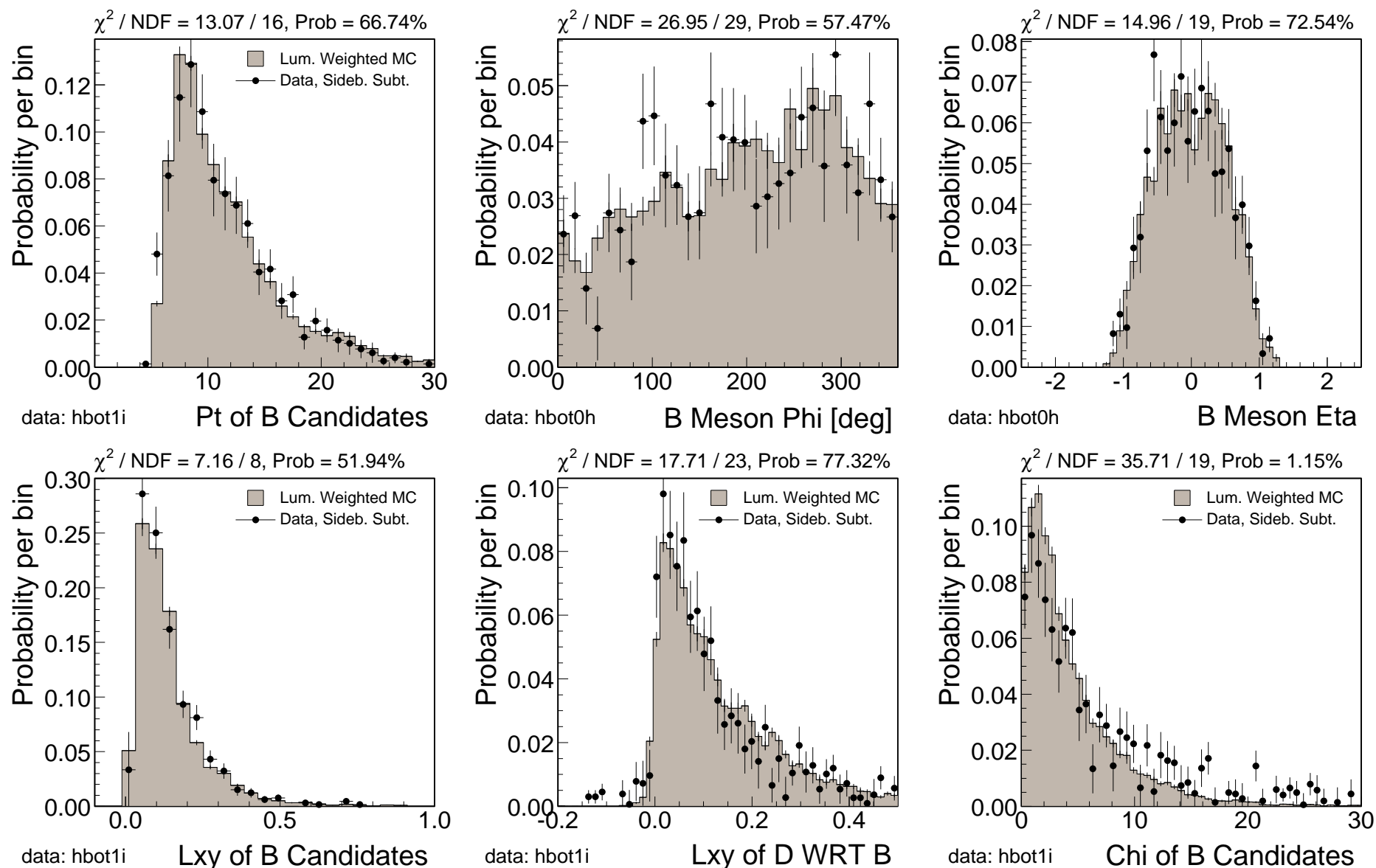


# Monte Carlo Validation Method



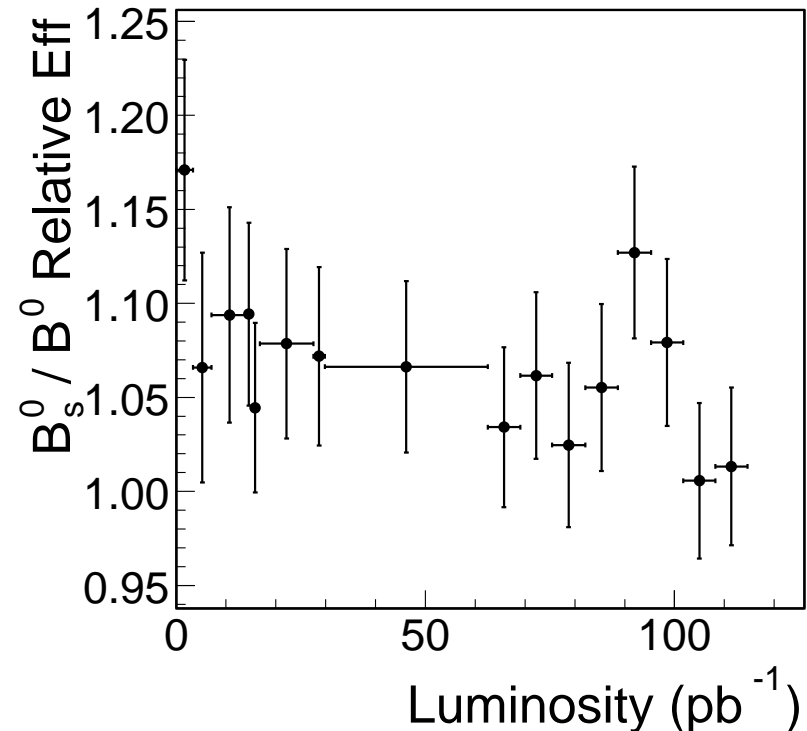
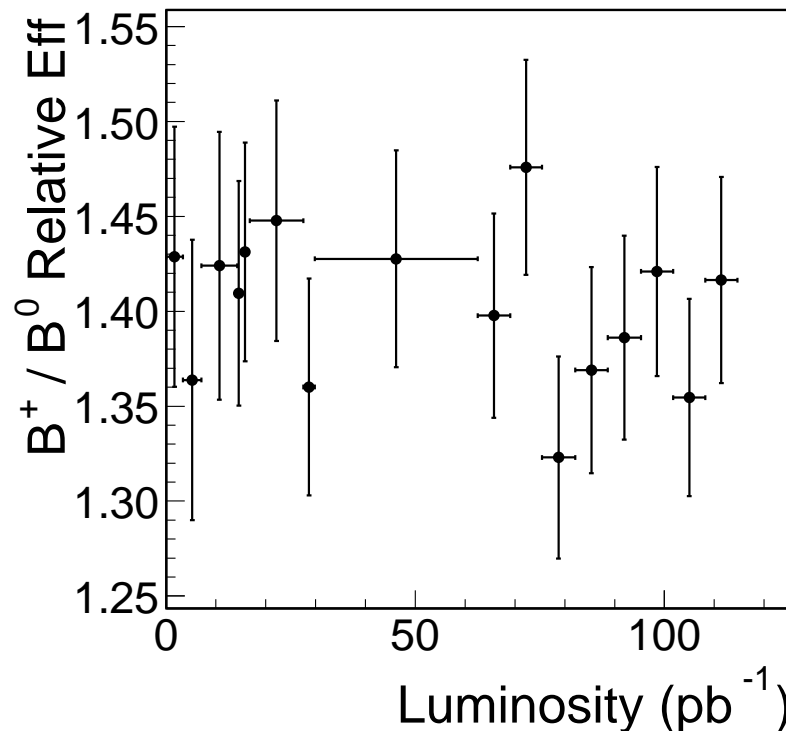
- high and low-mass sideband: **different composition**
- subtract **only** high-mass sideband
- but scale up number of events  
(using the exponential fit for the comb. background)
- check relevant distributions for both  $B^0$  and  $B^+$
- in addition, check N-1 cut efficiencies

# Monte Carlo Validation



● check many variables, good agreement for most

# Stability of Efficiency Ratios:



- trigger was constantly being upgraded
- concern: this may affect the efficiencies
- the ratio of total efficiencies is stable  
regardless of trigger efficiency change
- measurement quite robust to trigger conditions

# Systematic Uncertainties:

Effect	Syst. Unc.
$B$ $p_T$ spectrum	$\pm 1.5$ %
XFT simulation	$\pm 0.1$ %
$\phi^0$ mass cut	$\pm 1.0$ %
cut efficiencies	$\pm 5.0$ %
$B_s^0$ lifetime	$\pm 1.4$ %
$D_s^+$ lifetime	$\pm 0.3$ %
$B^0$ lifetime	$\pm 0.4$ %
$D^+$ lifetime	$\pm 0.04$ %
$B_s^0$ fitting	$\pm 5.0$ %
$B^0$ fitting	$\pm 7.0$ %
Total	$\pm 10.2$ %

# Measurement Results:

$$\frac{f_s}{f_d} \cdot \frac{Br(B_s^0 \rightarrow D_s^- \pi^+)}{Br(B^0 \rightarrow D^- \pi^+)} = 0.35 \pm 0.05(stat) \pm 0.04(syst) \\ \pm 0.09(BR)$$

Using the world average value for  $\frac{f_s}{f_d}$  ( $\frac{f_s}{f_d} = 0.26 \pm 0.03$ ) we obtain:

$$\frac{Br(B_s^0 \rightarrow D_s^- \pi^+)}{Br(B^0 \rightarrow D^- \pi^+)} = 1.4 \pm 0.2(stat) \pm 0.2(syst) \\ \pm 0.4(BR) \pm 0.2(PR)$$

Our measurement assumes the same fragmentation model for  $B_s^0$  and  $B^0$  mesons.

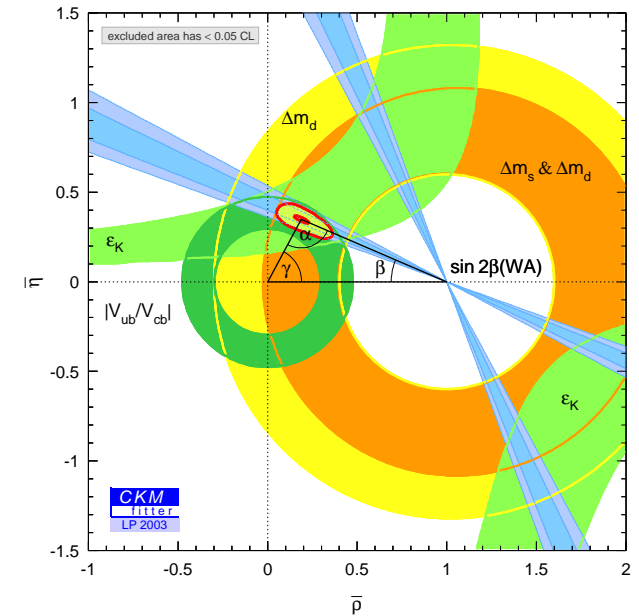
... now we can estimate our  $B_s$  mixing reach

# $B_s^0$ Mixing Reach Estimates

- **Current performance:**
  - $S = 1600/\text{fb}^{-1}$ ,  $S/B = 2 : 1$
  - $\epsilon D^2 = 4\%$ ,  $\sigma(ct) = 67 \text{ fs}$
- 
- **With “modest” improvements:**
  - $S = 2000/\text{fb}^{-1}$ ,  $S/B = 2 : 1$   
(improve trigger, more modes)
  - $\epsilon D^2 = 4\%$ ,  $\sigma(ct) = 50 \text{ fs}$   
(event by event prim vertex, Si on beampipe)
  - **$3\sigma$  sensitivity for  $\Delta m_s = 18 \text{ ps}^{-1}$  with  $1.3 \text{ fb}^{-1}$**
  - **$5\sigma$  sensitivity for  $\Delta m_s = 18 \text{ ps}^{-1}$  with  $1.7 \text{ fb}^{-1}$**
  - **$5\sigma$  sensitivity for  $\Delta m_s = 24 \text{ ps}^{-1}$  with  $3.2 \text{ fb}^{-1}$**
  - **this is a difficult measurement**

# Conclusions

- $B_s$  mixing at CDF II at a glance:
- initial work has begun
- reconstructed signal mode, understand rate
- work on tagging currently in progress, promising
- not a particle discovery,  $3\sigma$  is relevant!
- → **we want to constrain the unitary triangle**
- expect to surpass world limit with **1 year** of data
- beyond that, need to work on  $ct$  resolution and taggers to further extend reach
- push for more luminosity and gather more data



# B Mixing: $p\bar{p}$ vs $\Upsilon(4S)$

Quantity	$\Upsilon(4S)$	$p\bar{p}$
Mixing B Mesons	$B^0$	$B^0, B_s^0$
$\sigma(B)$	$\sim 1 \text{ nb}$	$\sim 100 \mu\text{b}$
$\sigma(B)/\sigma(\text{other})$	$\sim 1 : 5$	$\sim 1 : 1000$
ct resolution	$\sim 1.1 \text{ ps}$	$\sim 70 \text{ fs}$
tag. power ( $\epsilon D^2$ )	$\sim 30\%$	$\sim 5\%$

- higher B production cross section, produce  $B_s$
- immersed in light quark background
- triggering much more important
- B's boosted in the transverse plane
- less production flavor information